

Electrical Engineering

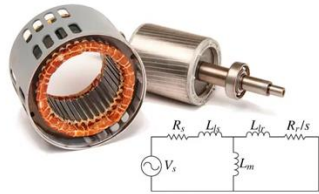


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Year 2023/2024



Introduction

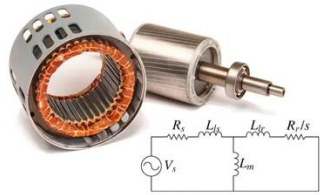
Schedule

	M1 AESM
Lectures	9 x 1 h15 + 2 DS
Tutorials	8 x 1,25 h
Lab work	1 x 2,50 h + 6 x 3,75 h

Outline

Introduction

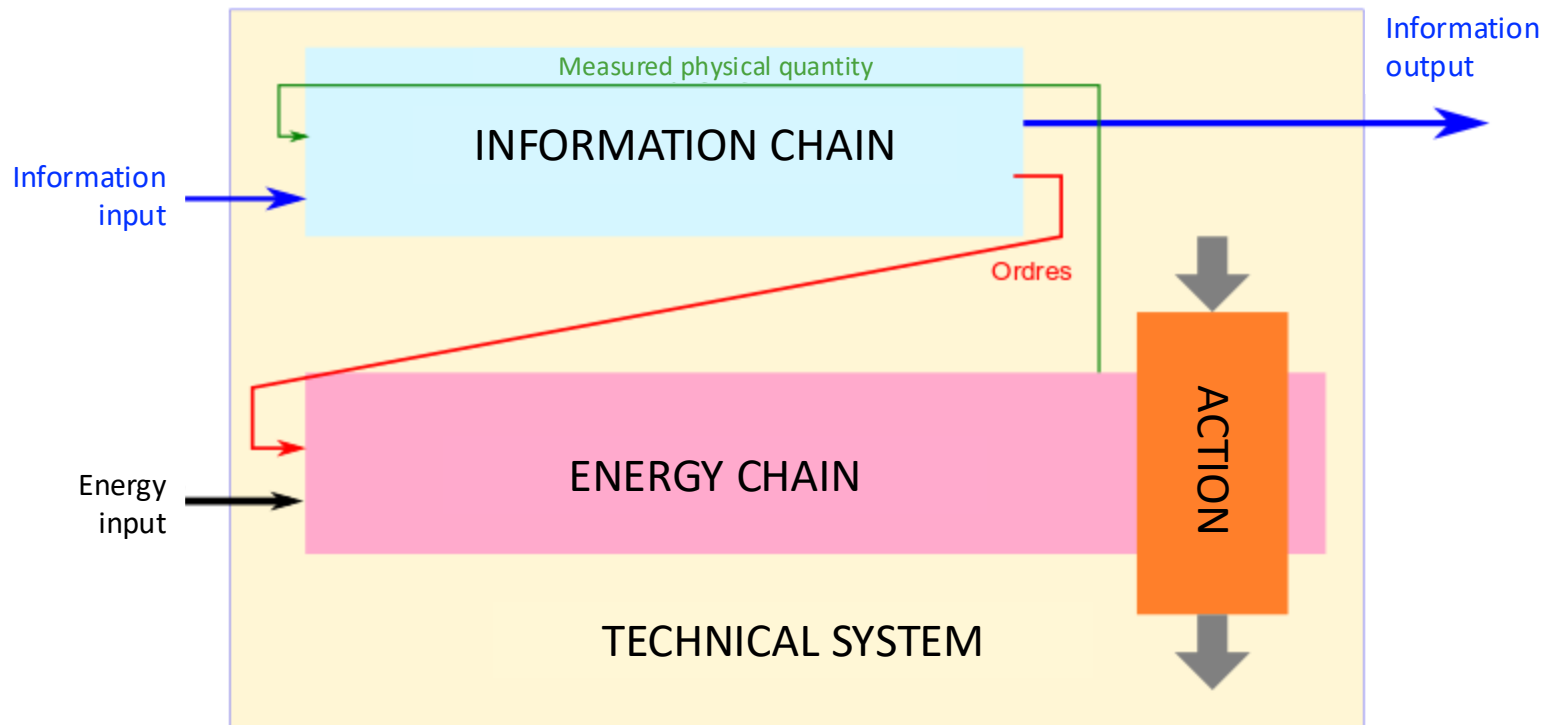
- I) Reminders (electricity)
- II) Power in sinusoidal regime (single-phase and 3-phase)
- III) Transformers
- IV) Electric motors

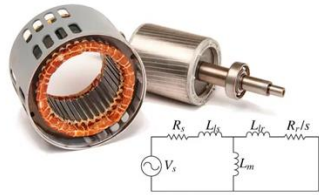


Introduction

Functional chain systems

- Technical systems, mechatronic systems, industrial systems





Introduction

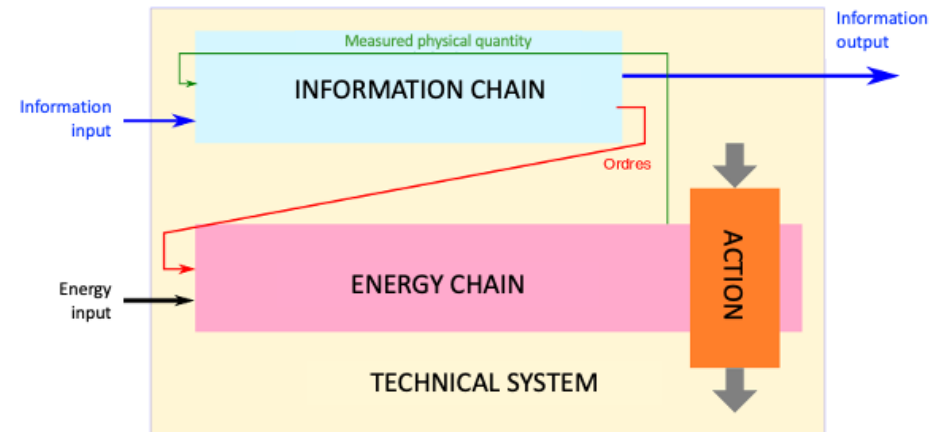
Electricity related fields

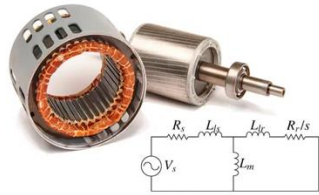
Electronics:

- ⇒ Current **lower** than 1 A
- ⇒ Information chain: data flow management

Electrical engineering:

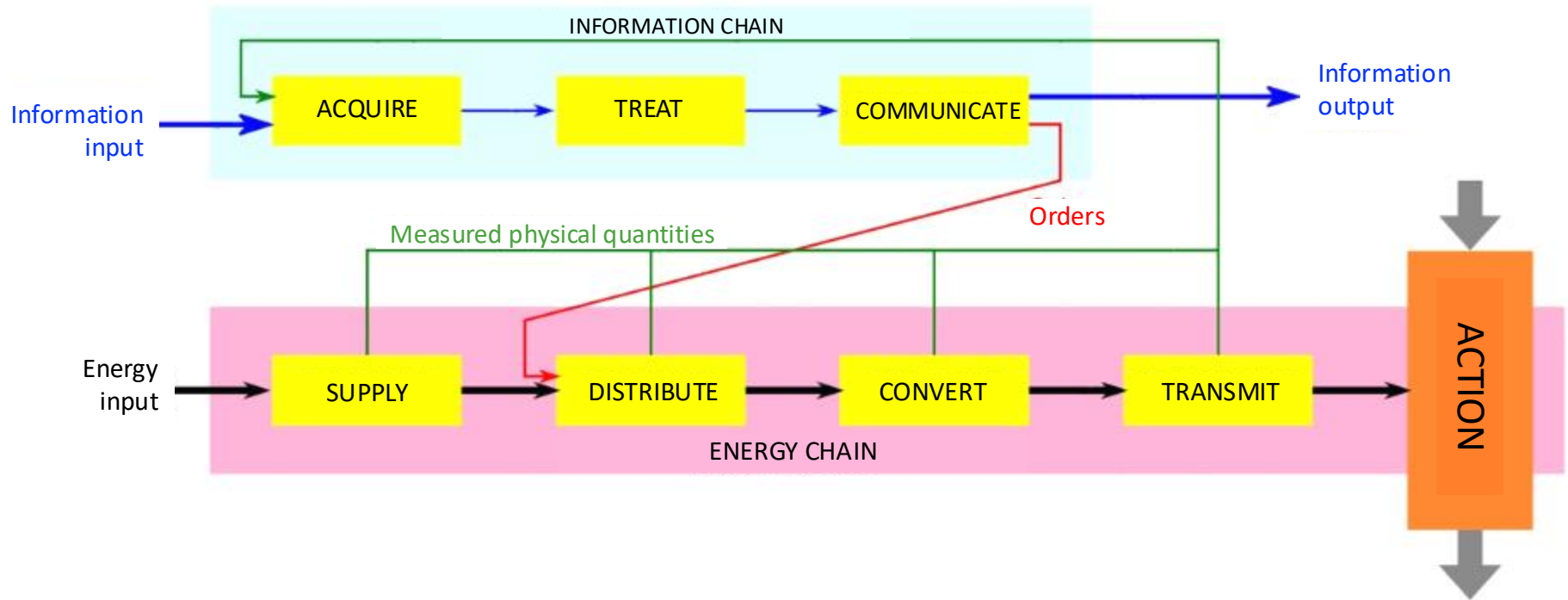
- ⇒ Current **higher** than 1 A
- ⇒ Energy chain: energy flow management

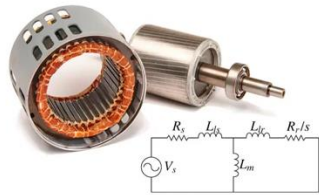




Introduction

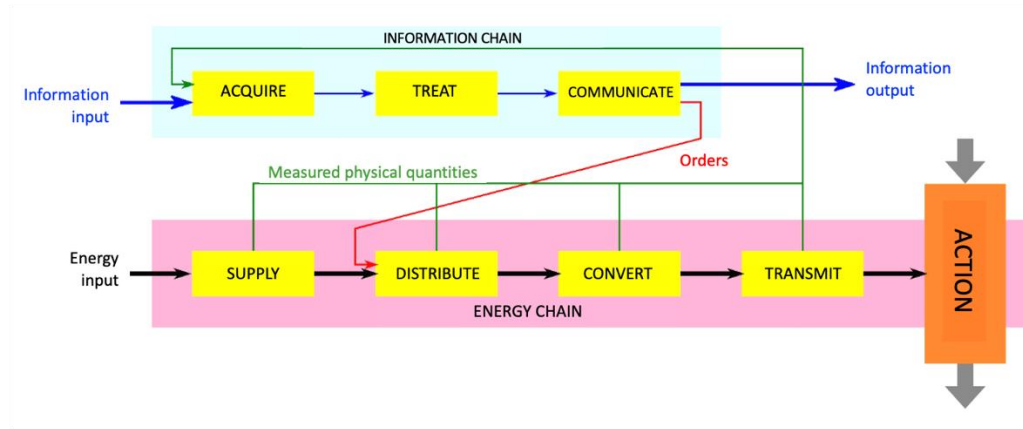
Energy chain



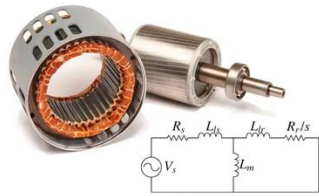


Introduction

Energy chain



Supply	Distribute	Convert	Transmit
<ul style="list-style-type: none"> • Production • Transport • Distribution • Installation design • Storage • Embedded power supply 	<ul style="list-style-type: none"> • Equipement • Motor start • Power electronics 	<ul style="list-style-type: none"> • Electric motors • Lighting • Electrothermics 	<ul style="list-style-type: none"> • Motion transformation • Light transmission • Heat transfert



Introduction

From primary energy to its use

- Energy utility:



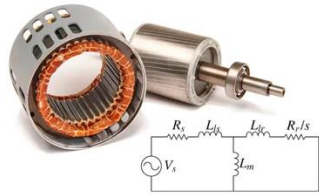
HEAT

WORK



LIGHT

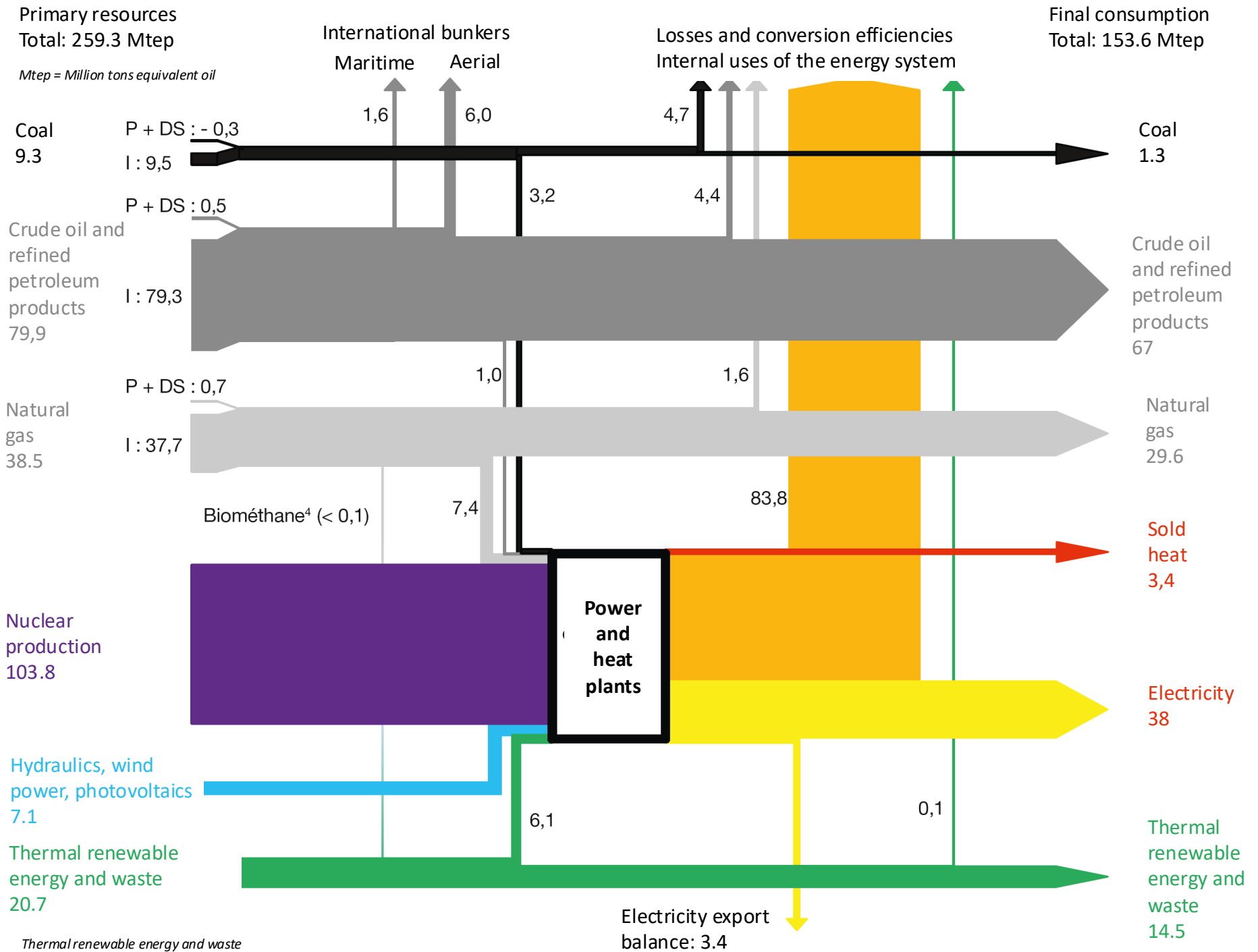
COMMUNICATION

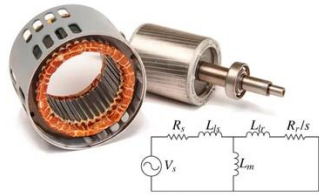


Introduction

From primary energy to its use

Primary energies	Storage	Carriers	Use
Non-renewable fossil fuels <ul style="list-style-type: none"> • Oil • Natural gas • Coal • Uranium 	Natural or controlled storage	Oil products	HEAT
Continuous renewable energies <ul style="list-style-type: none"> • Biomass • Urban waste • Geothermal energy • Hydraulic energy (dam, tidal power, water turbine) 	Natural or controlled storage	Gas	WORK
Non continuous renewable energies <ul style="list-style-type: none"> • Solar energy (thermal, photovoltaics) • Wind energy 	Mandatory storage in another form of energy	Electricity	LIGHT
		Steam	
		Compressed air	
		Hydrogen	
		Microwaves	COMMUNICATION




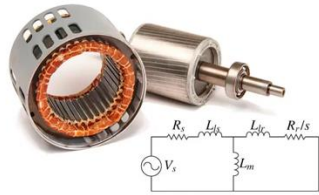


Introduction

Energy: 4 activities, many actors

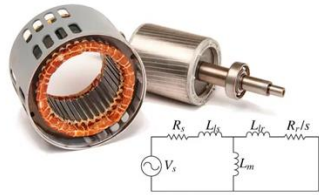
Franch law of February 10th,
2000

Production	EDF, Engie, E.On	Competitive business
Transport	French power grid	Regulated business
Distribution	ENEDIS (ex ERDF), public companies	Regulated business
Marketing	EDF, Engie, Poweo, Direct Énergie, ...	Competitive business
Inspection authority	French Energy Regulatory Commission	



Electrical energy

- Consumed as soon as it is produced
- Distributed instantly to the point of use
- No mass storage is currently possible



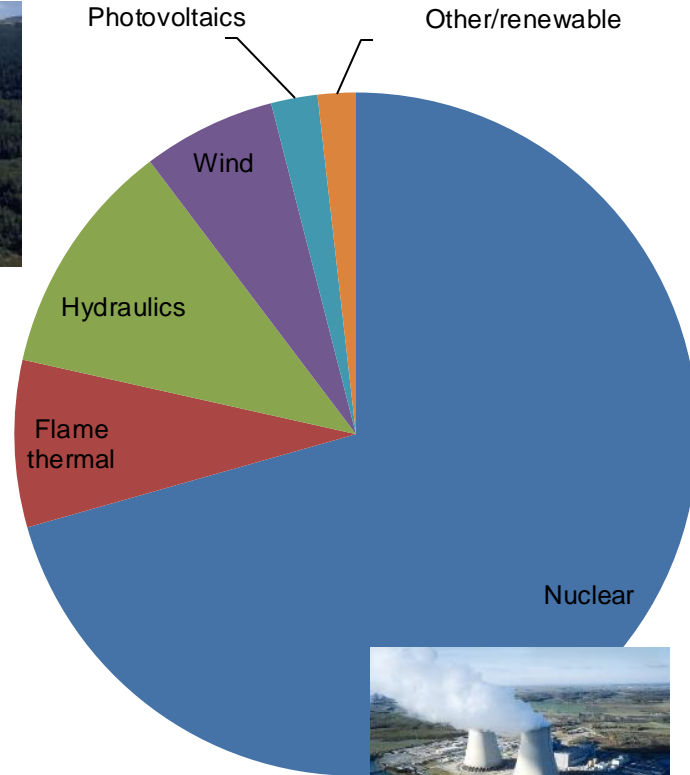
Introduction

Electricity production in France

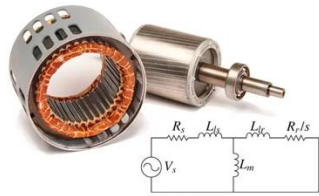


**In 2019 : 538 TW.h
(46,3 Mtep)**

- Nuclear: 70,6 %
- Flame thermal: 7,9 %
- Hydraulics: 11,2 %
- Wind: 6,3%
- Photovoltaics: 2,2 %
- Other/renewable: 1,8 %



132 MTEp were required to produce these 46 MTEp.



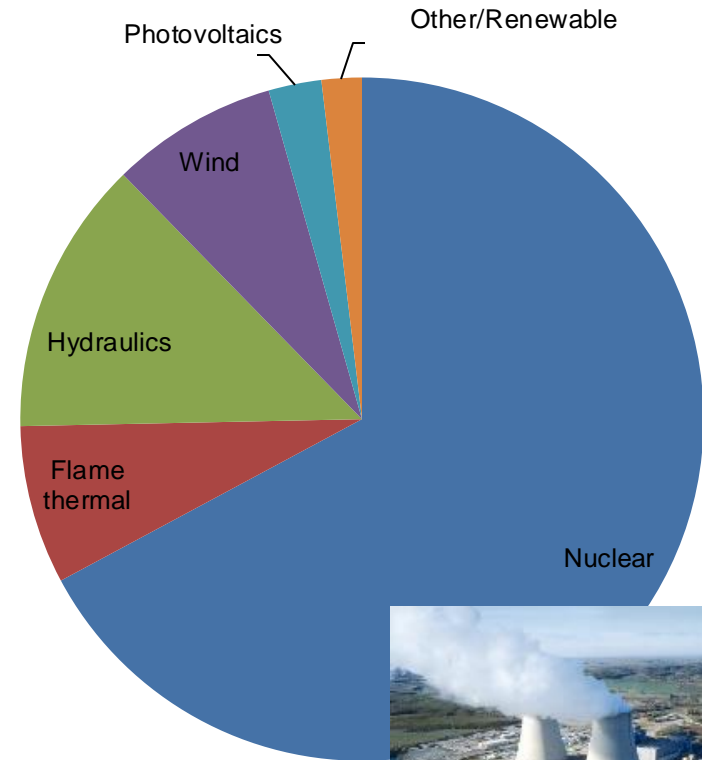
Introduction

Electricity production in France

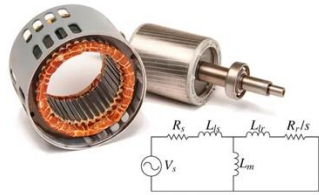


In 2020 : 500 TW.h
(2,7 Mtep)

- Nuclear : 67,1 %
- Flame thermal: 7,5 %
- Hydraulics : 13 %
- Wind : 7,9%
- Photovoltaics : 2,5 %
- Other/Renewable: 1,9 %



123 MTEp were **required** to produce these **43 MTEp**.



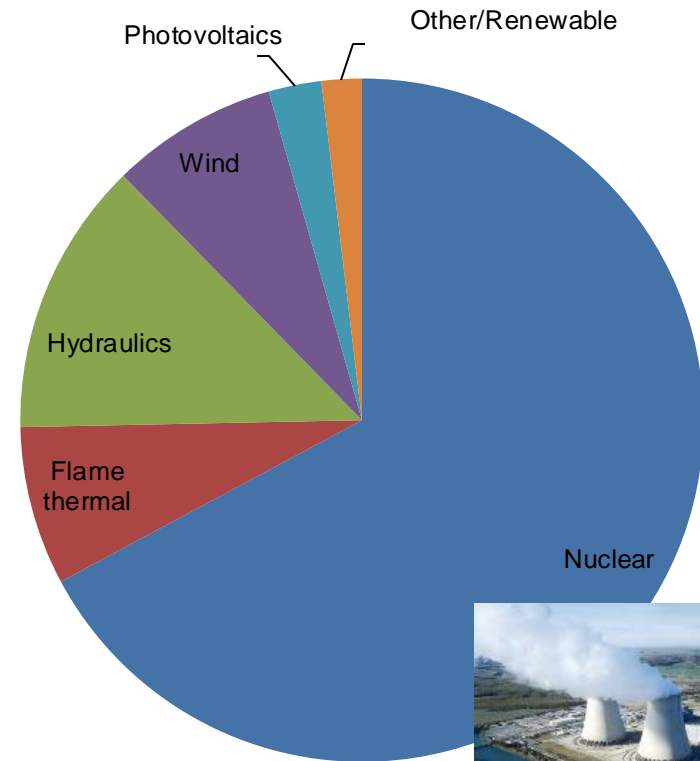
Introduction

Electricity production in France

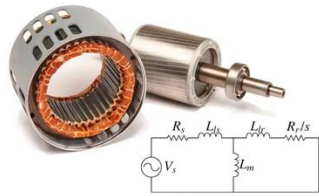


**In 2021 : 523 TW.h
(45 Mtep)**

- Nuclear : 69 %
- Flame thermal: 7,4 %
- Hydraulics : 12 %
- Wind : 7%
- Photovoltaics : 2,7 %
- Other/renewable : 1,9 %



129 MTEp were required to produce these 45 MTEp.



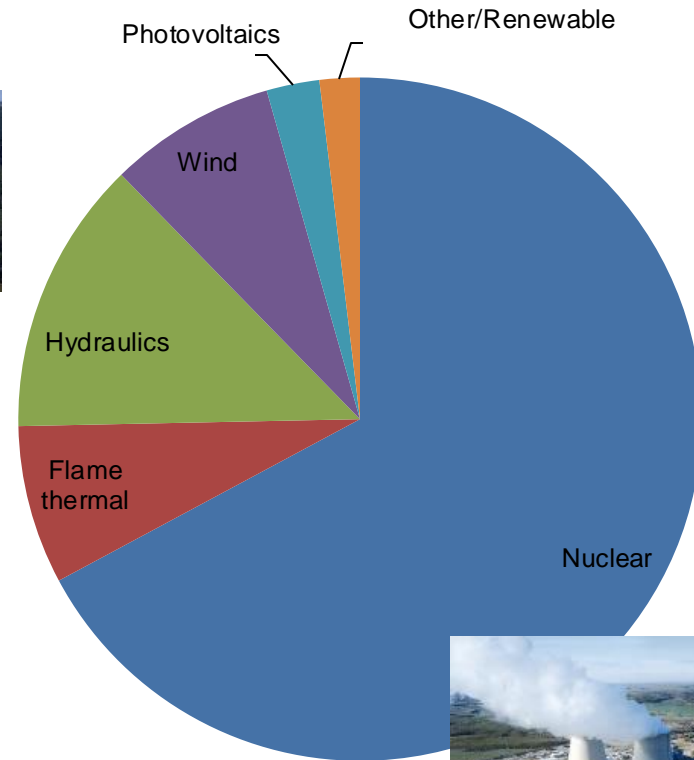
Introduction

Electricity production in France

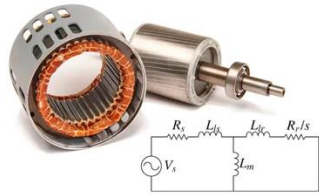


In 2022 : 445 TW.h
(38,3 Mtep)

- Nuclear: 62,7 %
- Flame thermal: 11,1 %
- Hydraulics: 11,1 %
- Wind: 8,6%
- Photovoltaics: 4,2 %
- Other/Renewable: 2,4 %

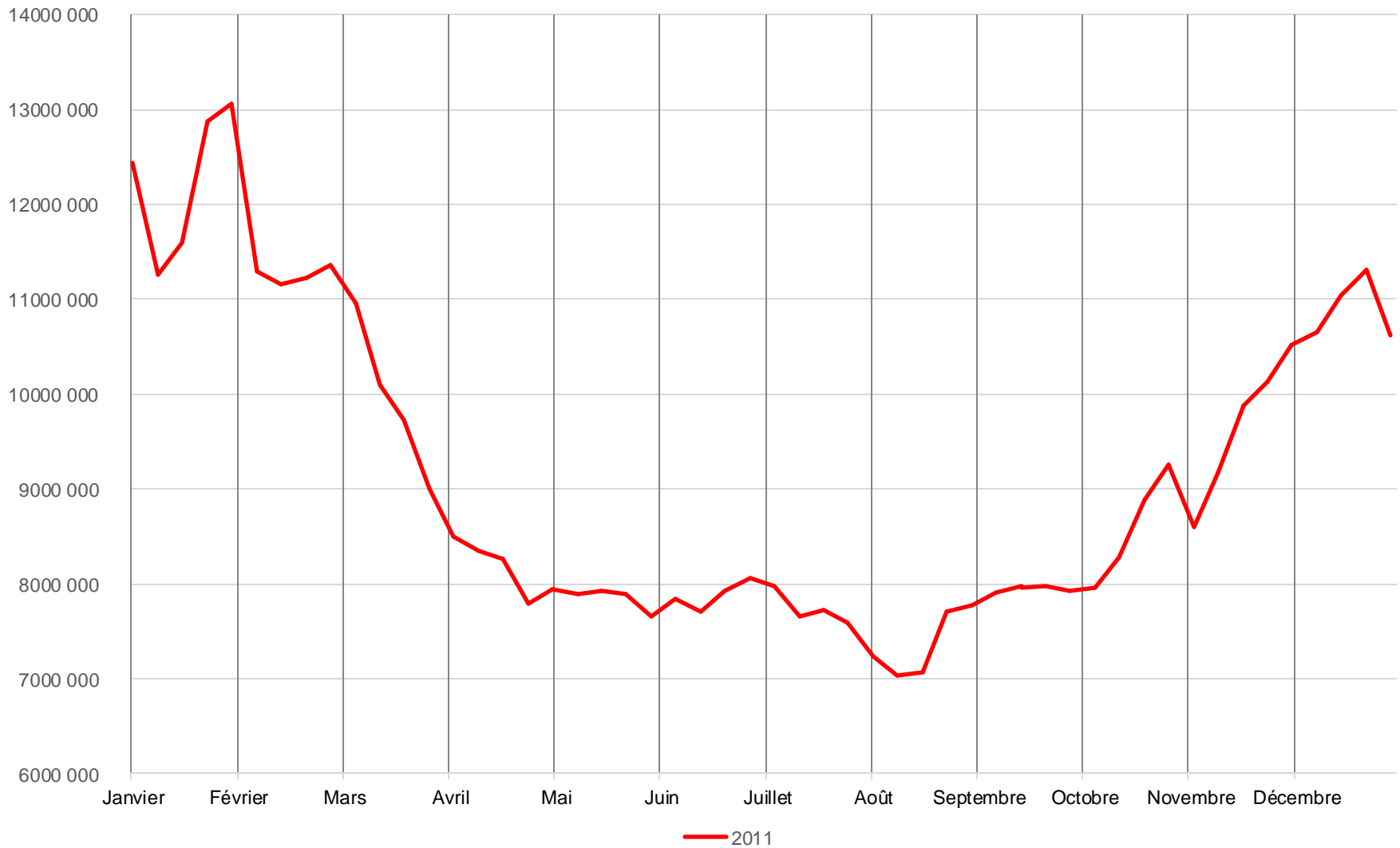


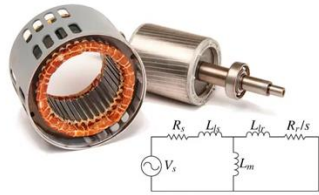
110 MTEp were **required** to produce these **45 MTEp**.



Introduction

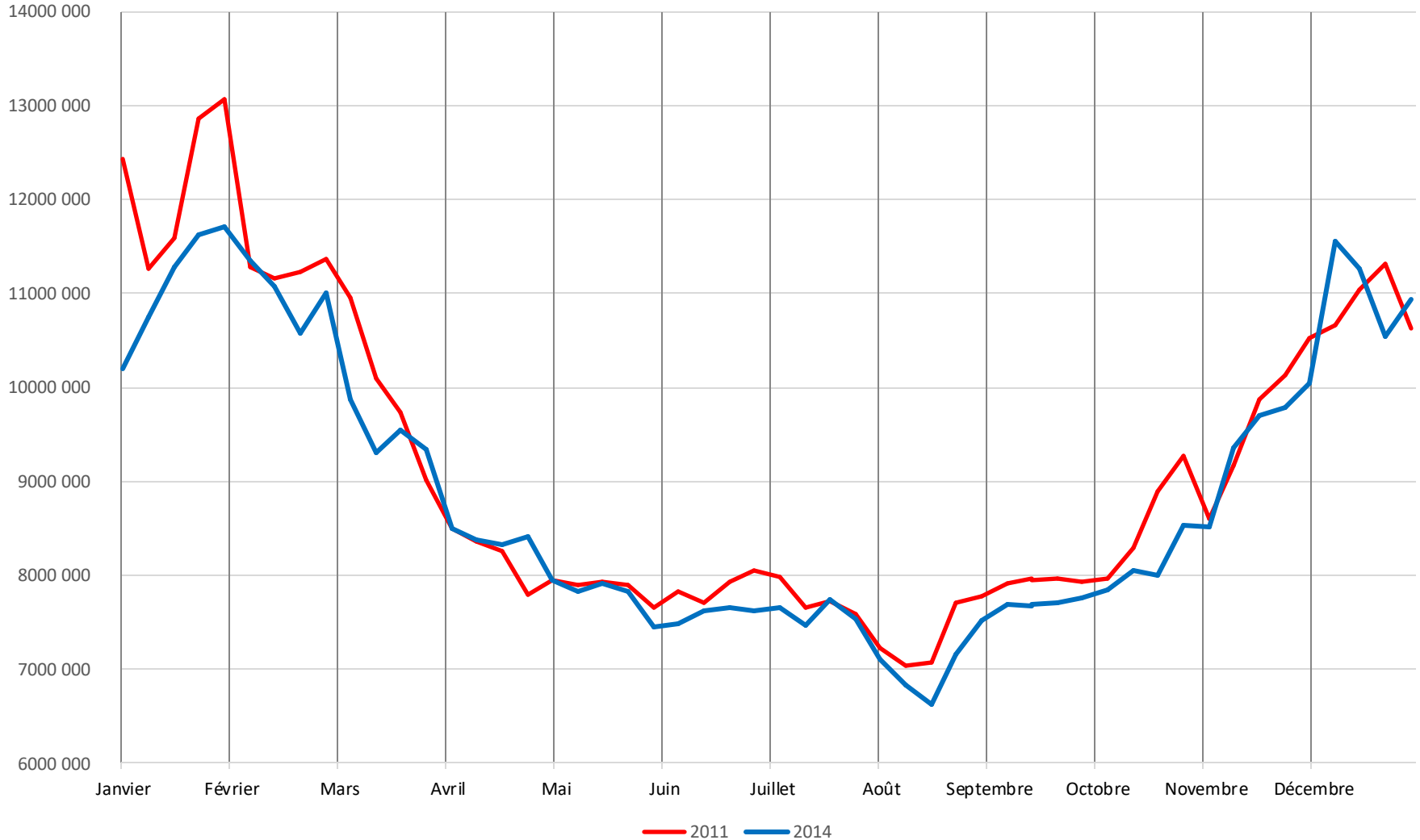
Electricity consumption in France in 2011 (in MW.h)





Introduction

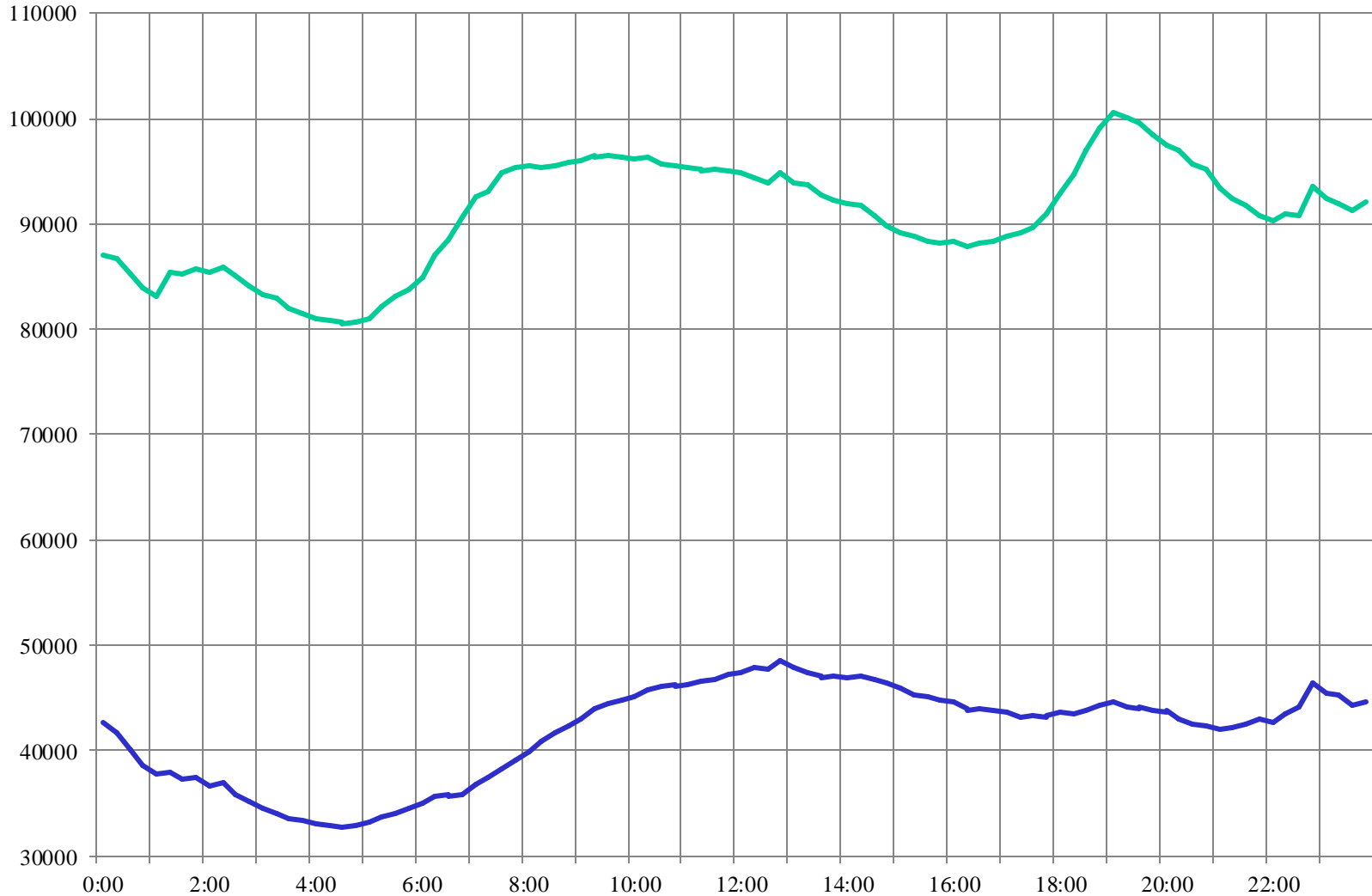
Electricity consumption in France in 2011 and 2014 (in MW.h)

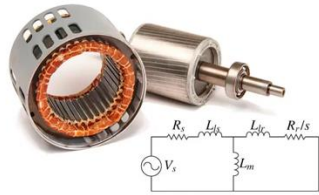




Introduction

Electricity consumption on 7/02/2024 and 7/08/2024 in France (in MW)

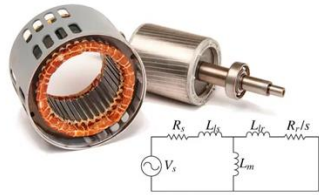




Introduction

Real time production in France

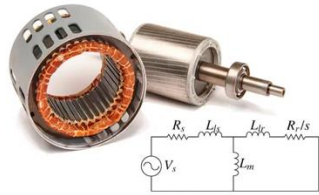
<https://www.rte-france.com/eco2mix/la-production-delectricite-par-filiere#>



Electrical energy production in France

- “Grand Maison” dam





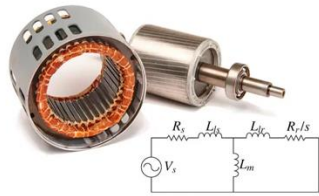
Electrical energy production in France

- “Grand Maison” dam

Pumped-storage power station

- Gravity dam, 550 m long et 140 m high (160 m on foundation),
- Reservoir 137 millions m³ water
- Built at 1700 m altitude from 1978 to 1988
- Flow: **216 m³/s** (76 and 140 m³/s)
- Drop height: **922 et 955 m**
- Verney plant : **12 turbo-alternators of 153 MW** – 15500V, Pelton turbines
- Total installed power: **1820 MW** equivalent to **two nuclear units**.
- Extraction : 6 elevating transformers 15500V / 405000V

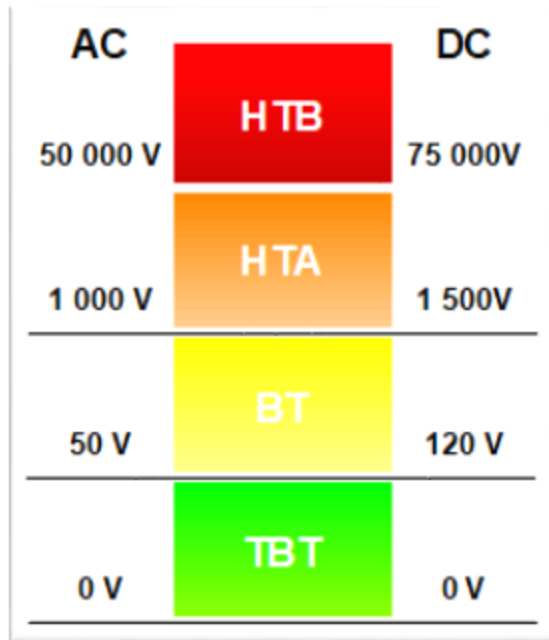




Introduction

Electrical voltage ranges in France

- HTA and HTB: High voltage (“Haute Tension”)
- BT: Low voltage (“Basse Tension”)
- TBT: Very low voltage (“Très Basse Tension”)



HTB



TBT

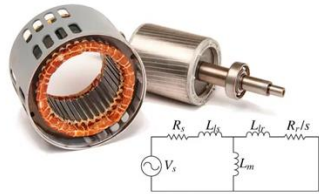


HTA



BT

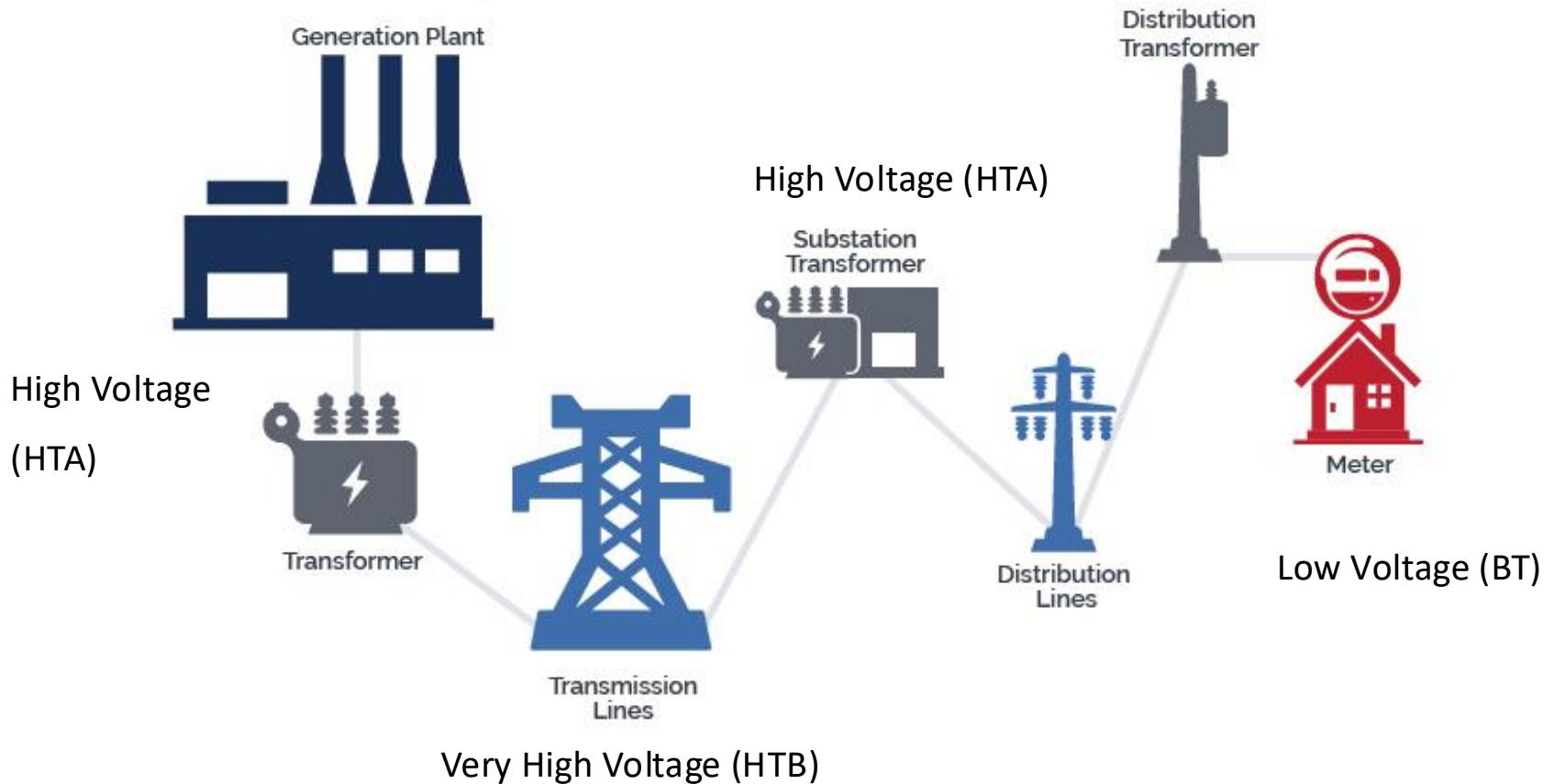




Introduction

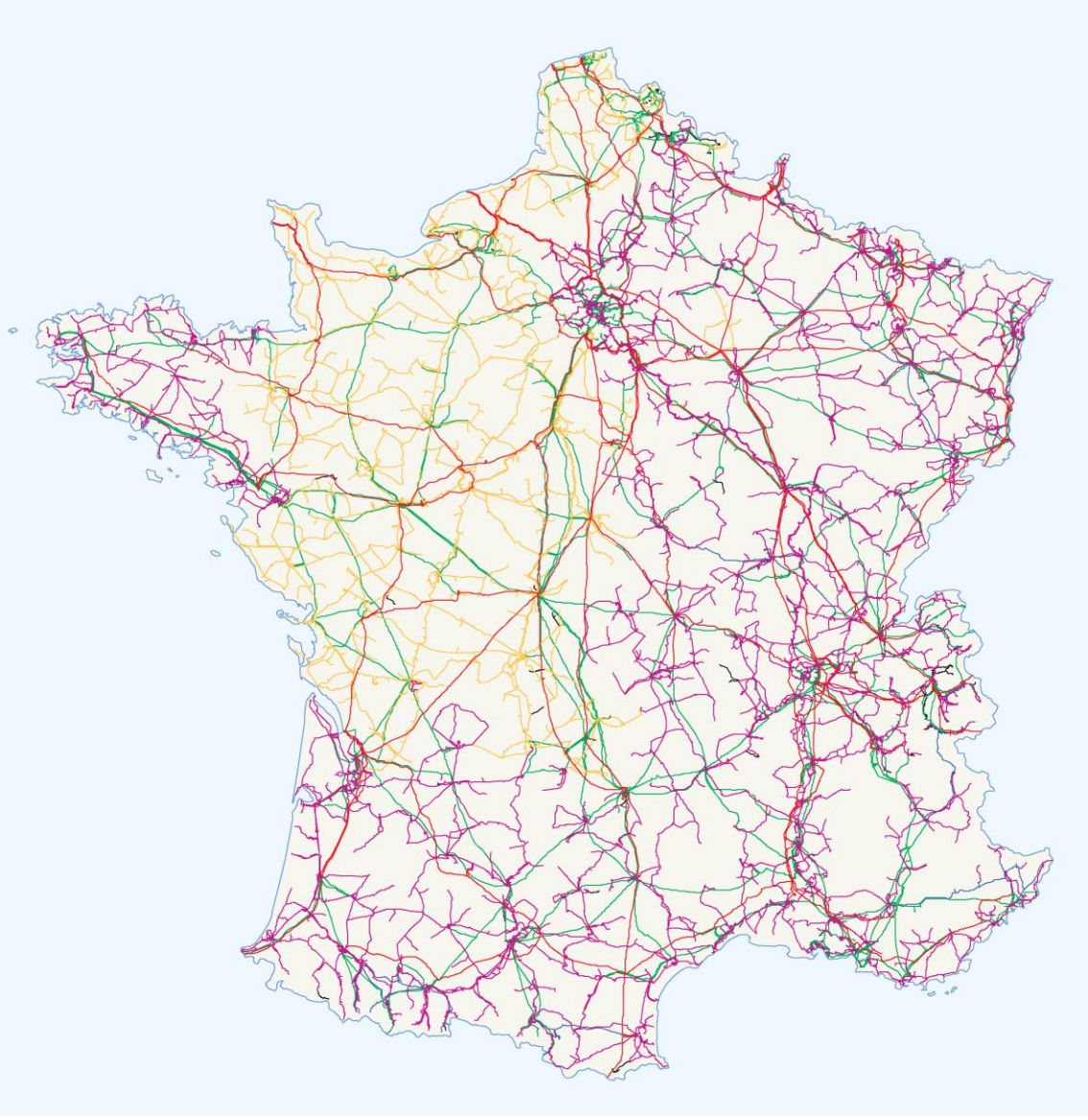
Power grids : basic structure

The Electric Utility Network





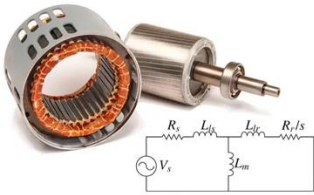
Introduction



Distribution RTE grid



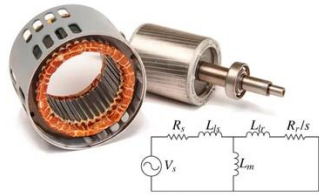
1.6 million km long



Introduction

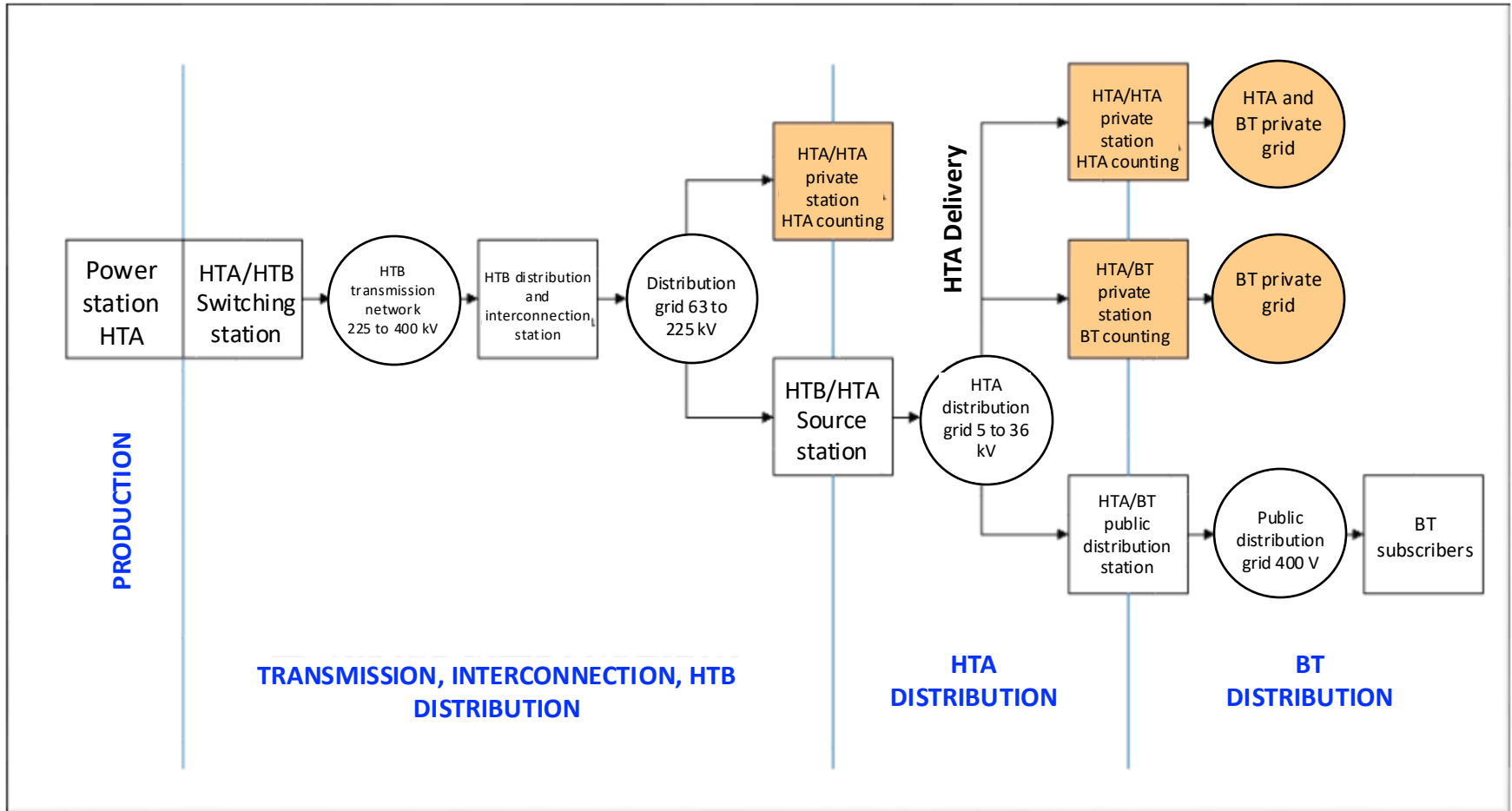
RTE grid 400 kV

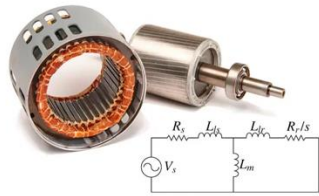




Introduction

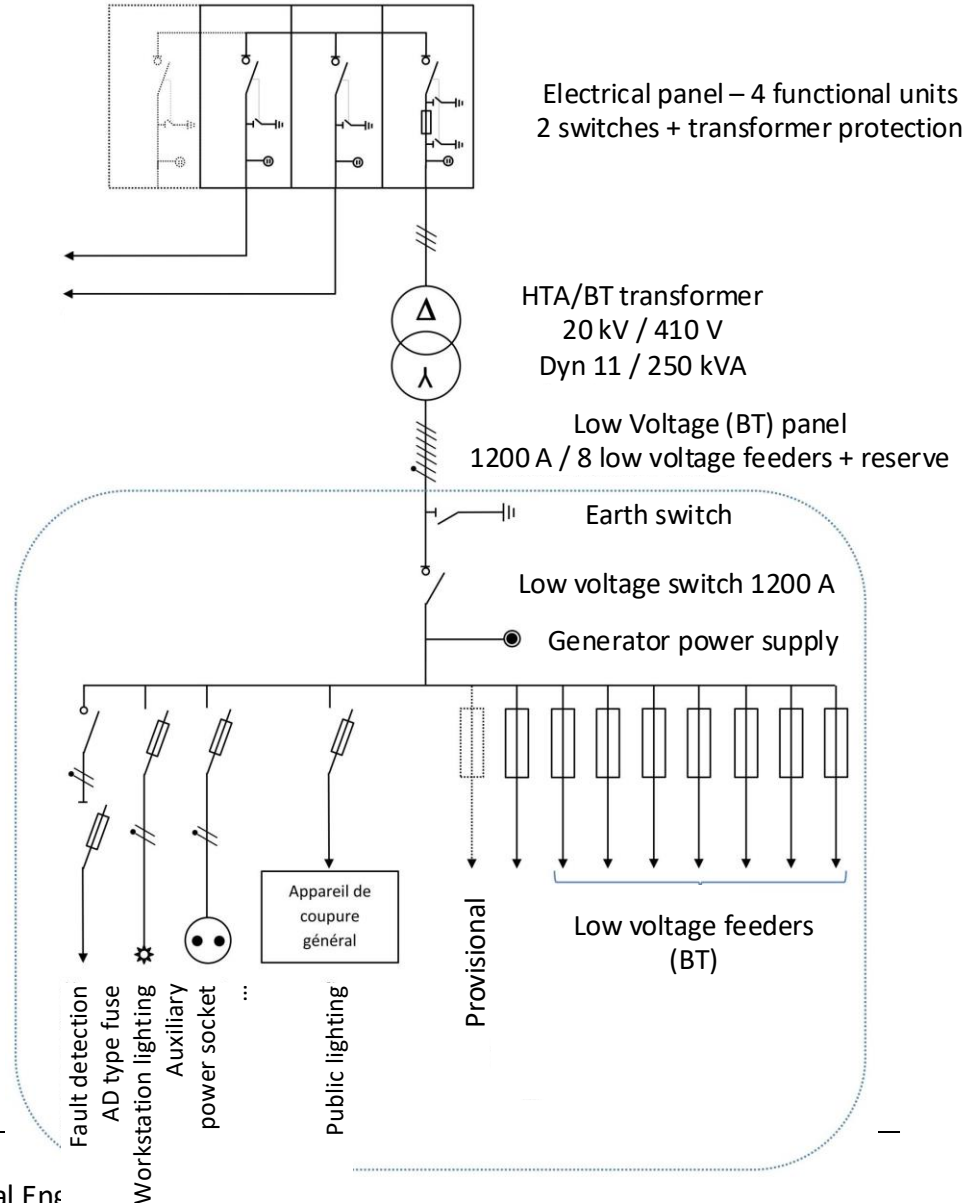
Network interconnection



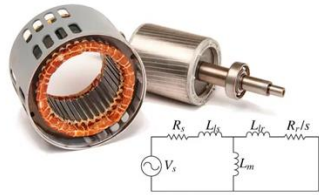


Introduction

- Urban transformer station HTA/BT



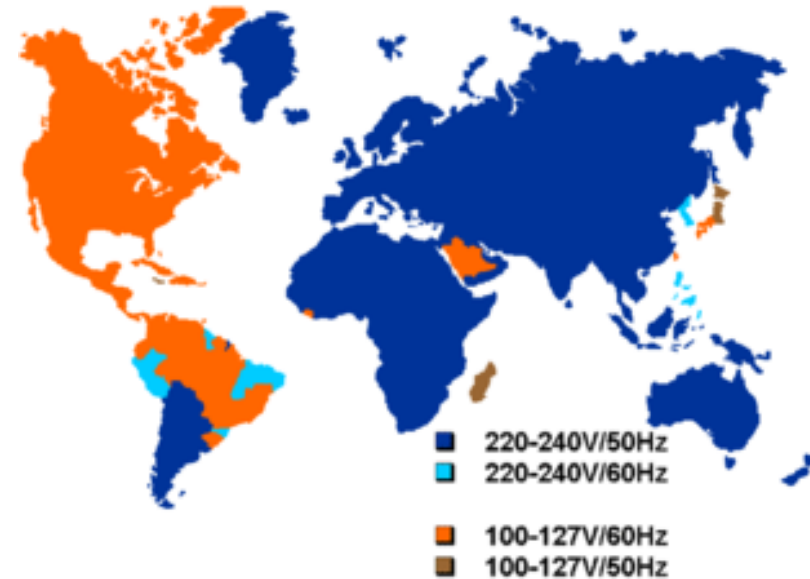
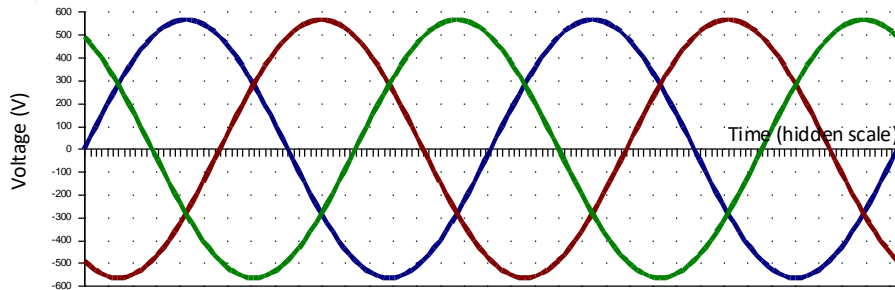
Electrical Eng



Introduction

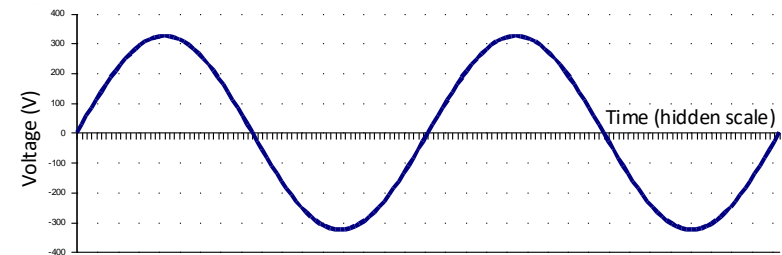
Distribution

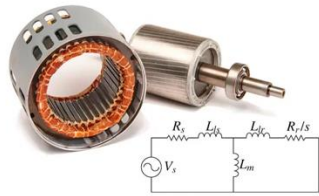
- In France, **three-phase distribution** 400 V/230 V at 50 Hz (sine-wave)



- In the world, both voltage and frequency can be slightly different
- Delivery to the customer : **single-phase** distribution

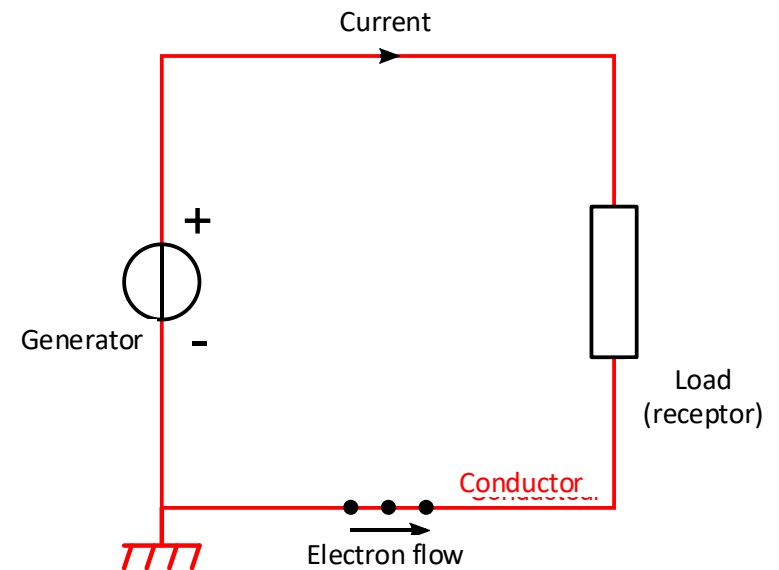
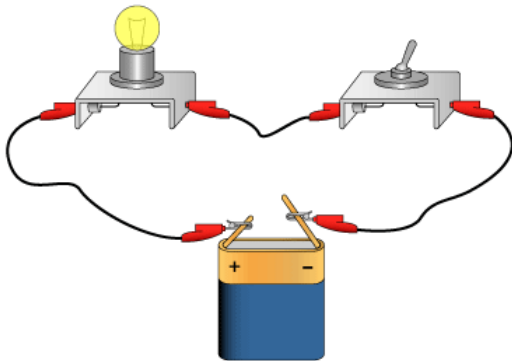
=> In France: 230 V, 50Hz

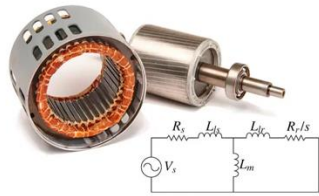




The electrical circuit

- **Electrical circuit** = electrical generator + load(s) (electrical receptor)
- Each element of the circuit is connected by metal conductors (usually copper wires)
- => When the circuit is closed, the generator makes the electrical charges flow





I - Reminders

Electric quantities

Electrical current

- Electrical current $i(t)$ = electrical charge $q(t)$ flow

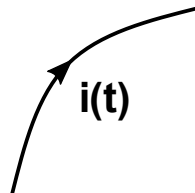
$$i(t) = \frac{dq(t)}{dt}$$

- $i(t)$ characterized by its **direction** and its **intensity**

=> $i(t)$ is measured in **Amperes** (A)

- $i(t)$ has the same value at each point of a single circuit

=> No charge accumulation at one point, the flow is the same everywhere



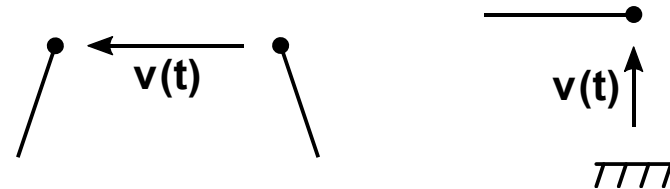
Voltage

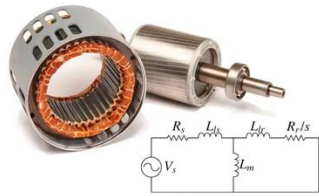
-The electrical generator creates a **potential difference** that makes electrical charges flow through the circuit

- **Voltage** $v(t)$ = potential difference

=> $v(t)$ is measured in **Volts** (V)

- All voltages in a circuit are defined in relation to a reference zero potential usually called the **ground**





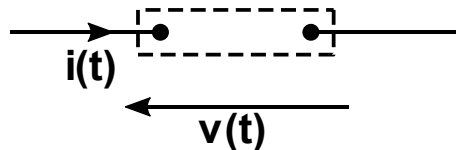
I - Reminders

Convention

- **Electric dipole** = element of the circuit having two terminals through which a current flows when a voltage is applied

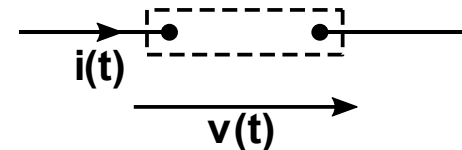
Receptor convention

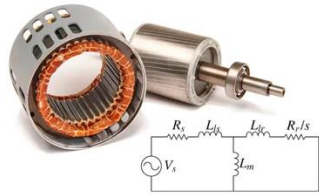
- Current and voltage in **opposite directions** for each **receptor**
- The dipole **receives** power



Generator convention

- Current and voltage in **same directions** for each **generator**
- The dipole **supplies or generates** power





I - Reminders

Electrical power

- A dipole exchanges energy with other dipoles to which it is connected. It can transform one form of energy into electrical energy, or convert electrical energy into another form of energy

- The exchanged or transformed energy written $dw(t)$ (in joule (J)), is related to the operating time written dt in second (s), by :

$$p(t) = \frac{dw(t)}{dt} \quad \text{with } p(t) \text{ the power in watt (W)}$$

- A receptor under a voltage $v(t)$ and carrying a current $i(t)$ generates or receives an instantaneous power $p(t)$.

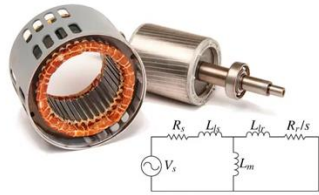
=> This power reflects the energy exchanges between the generator and the receptor at each instant t .

- The exchanged or transformed energy written $dw(t)$ (in joule (J)), is related to the operating time written dt in second (s), by :

$$p(t) = v(t) \times i(t)$$

- Current and voltage are algebraic quantities => power is also an algebraic quantity.

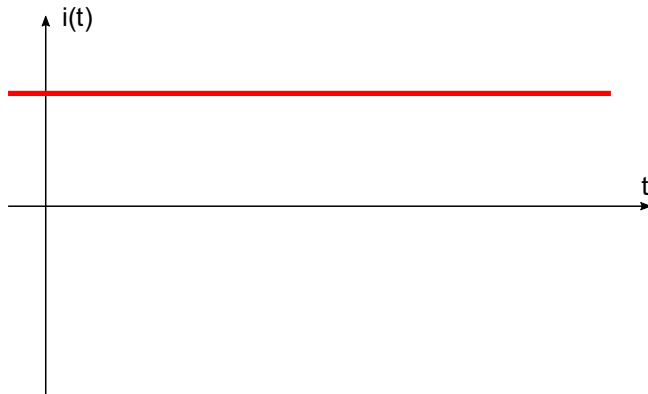
- With a given convention, generator or receptor, the nature of the dipole, generator or receptor, is the same as that of the convention if the sign of the power is positive.



I - Reminders

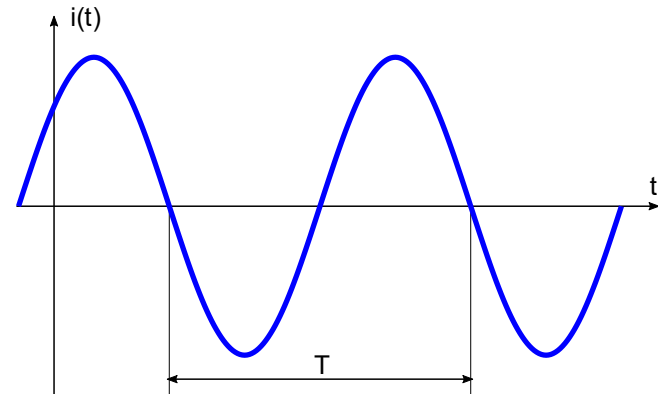
AC/DC operating regimes

DC current

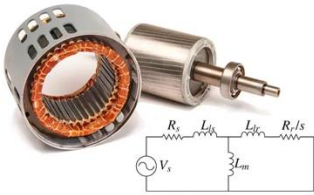


- Current intensity remains **constant** with time

AC current



- Intensity is variable and changes direction periodically.
- Period T is measured in seconds.
- Frequency f , number of periods described by the current in one second, measured in Hertz (Hz).
- Frequency of 50 Hertz in France and Europe.

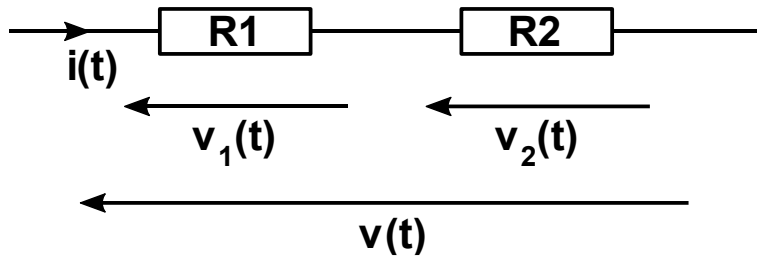


I - Reminders

Dipole connection

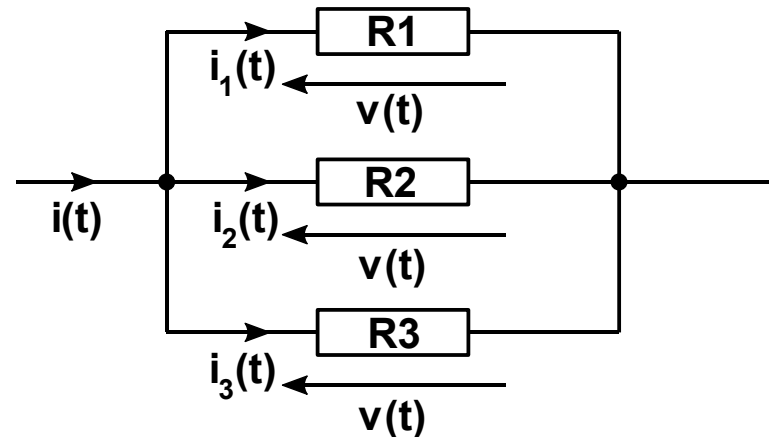
Receptors in series

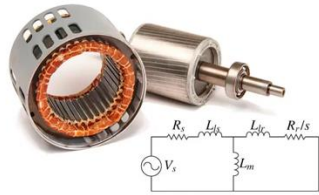
- Dipoles are connected in series when the same current flows through them



Receptors in parallel

- Dipoles are connected in parallel when they are subjected to the same voltage.





I - Reminders

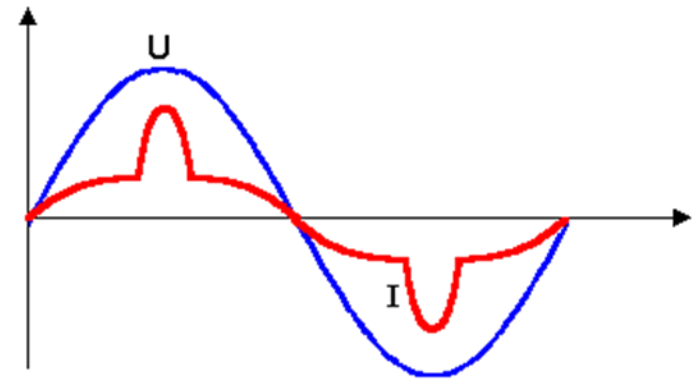
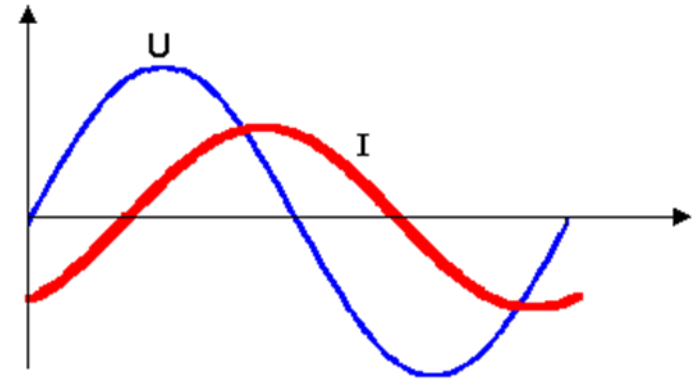
Linear dipoles

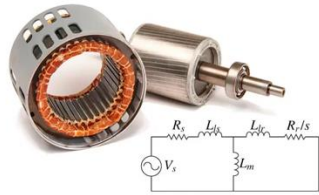
- A dipole is linear if the relation between the voltage at its terminals and the current flowing through it is linear.

$$v(t) = f(i(t))$$

- Function f is linear if:

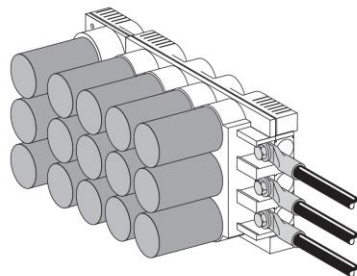
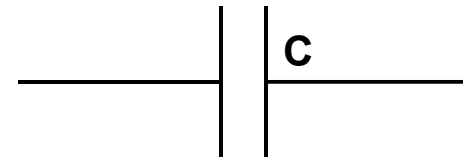
$$f(\alpha_1 \cdot i_1(t) + \alpha_2 \cdot i_2(t)) = \alpha_1 \cdot f(i_1(t)) + \alpha_2 \cdot f(i_2(t))$$

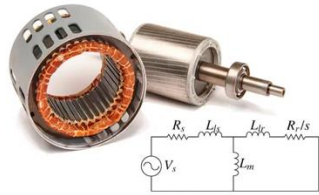




Passive dipoles

- A passive dipole is an electric component that dissipates or temporarily stores electrical energy.





I - Reminders

The resistor

- A **resistor** is an electric dipole that opposes the current. R , the resistance, is expressed in **Ohm** (symbol: Ω)

- **Ohm's law:**

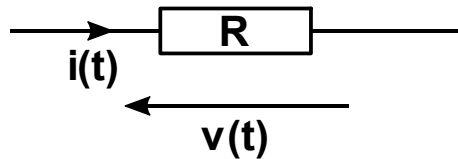
$$v(t) = R \cdot i(t)$$

R : resistance in Ω (Ohm)

$v(t)$: voltage across the resistor in V (Volt)

$i(t)$: current through resistor in A (Ampere)

- **Resistance symbol in receptor convention:**



- Remarks:

- G , the inverse of resistance, is called conductance and is expressed in Siemens (S).

$$i(t) = G \cdot v(t)$$

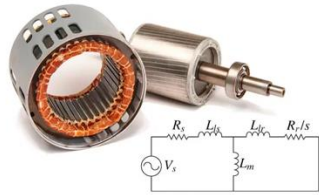
- Electric resistance in Ω :

$$R = \rho \times \frac{l}{s}$$

ρ : electrical resistivity in $\Omega \cdot m$

l : conductor length in m

s : conductor cross-section in m^2



The capacitor



- A **capacitor** is an electric dipole that opposes changes in voltage and can store energy in electrostatic form. C , the **capacitance** of a capacitor, is independent of time and is expressed in **Farads** (F).

- Relation between current and voltage:

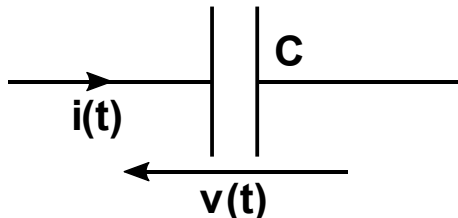
$$i(t) = C \cdot \frac{dv(t)}{dt}$$

C : capacitance in F (Farad)

$v(t)$: voltage across capacitor in V (Volt)

$i(t)$: current in A (Ampere)

- Relation between current and voltage:



- Remarks:

- We can also write:

$$V_C(t) = \frac{1}{C} \cdot \int i(t) \cdot dt$$

- No voltage discontinuity across a capacitor.

- Capacitance of a planar capacitor in Farad

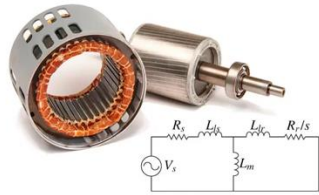
$$C = \epsilon_0 \cdot \epsilon_r \frac{S}{e}$$

ϵ_0 : vacuum permittivity (8.85×10^{-12})

ϵ_r : relative dielectric permittivity

S : surface area of armatures in m^2

e : dielectric thickness in m



The coil

- A **coil** is an electric dipole that opposes the variation of electric current and can store energy in electromagnetic form. L , the coil **inductance**, is independent of time and is expressed in Henry (H).

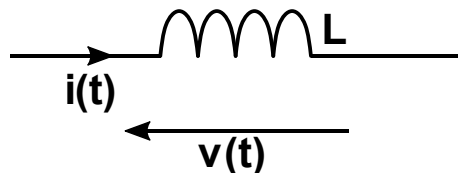
- Relation between voltage and current:

$$v(t) = L \cdot \frac{di(t)}{dt}$$

L : inductance in H (Henry)

$v(t)$: voltage across coil in V (Volt)

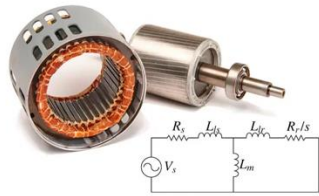
$i(t)$: current in A (Ampere)



- Remark:

- No discontinuity in the current flowing through an inductor.





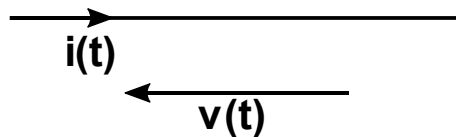
I - Reminders

Short and open circuits

The short circuit or the wire

- The **short-circuit**, the **wire**, the **closed contact** (switch or any other electric device) are dipoles with zero resistance. The **voltage** at their terminals is **zero**, whatever the current flowing through them.

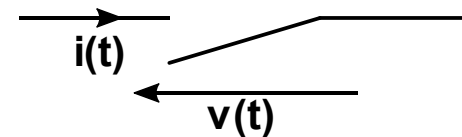
$$v = 0, \forall i$$

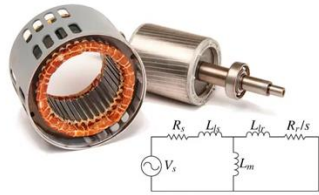


The switch or the open circuit

- The **open circuit**, the **cut wire** or the **open contact** (switch or other electric device) are dipoles with infinitely high resistance. The **current** flowing through them is **zero**, whatever the voltage at their terminals.

$$i = 0, \forall v$$





I - Reminders

Passive dipole power

- Time-dependent power:

$$p(t) = v(t) \times i(t)$$

- For a resistor:

$$p_R(t) = v(t) \cdot i(t) = R \cdot i^2(t)$$

- For a capacitor:

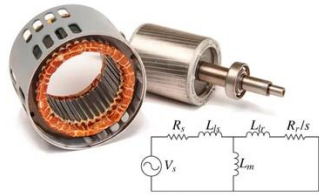
$$p_C(t) = v(t) \cdot C \cdot \frac{dv(t)}{dt} = \frac{1}{2} \cdot C \cdot \frac{dv^2(t)}{dt}$$

- For a coil:

$$p_L(t) = L \cdot \frac{di(t)}{dt} \cdot i(t) = \frac{1}{2} \cdot L \cdot \frac{di^2(t)}{dt}$$

- The power in a **resistor** is always positive. This dipole cannot restore it. It is said to be **dissipative** (Joule effect). => **active** component

- The power in a capacitor or a coil can be positive or negative. These two dipoles can **store** and **release energy**. They are said to be **reactive**.



I - Reminders

Passive dipole energy

- Energy of a dipole at time t:

$$w(t) = w(0) + \int_0^t p(x) dx$$

- For a resistor:

$$w_R(t) = R \cdot \int_{-\infty}^t i^2(x) dx$$

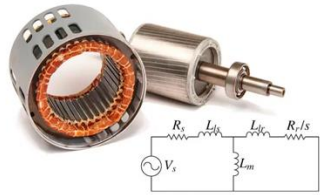
- For a capacitor:

$$w_C(t) = \frac{1}{2} \cdot C \cdot v^2(t)$$

- For a coil:

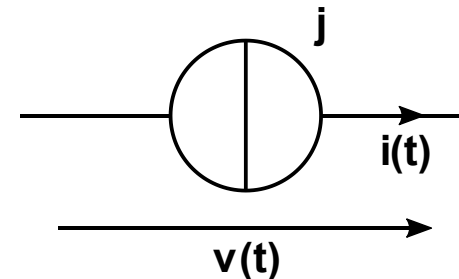
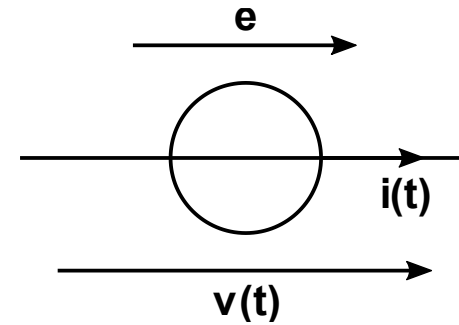
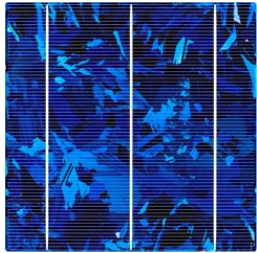
$$w_L(t) = \frac{1}{2} \cdot L \cdot i^2(t)$$

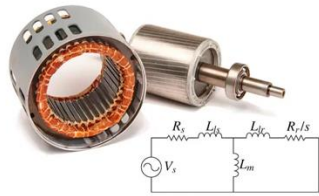
- **Energy** is **always positive**. This property is characteristic of passive elements



Active dipoles

- Dipole able to **supply energy** to a load connected to it. They are electrical or electronic components where **electromotive phenomena** can permanently convert electrical energy.

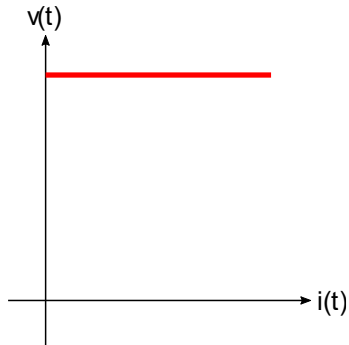




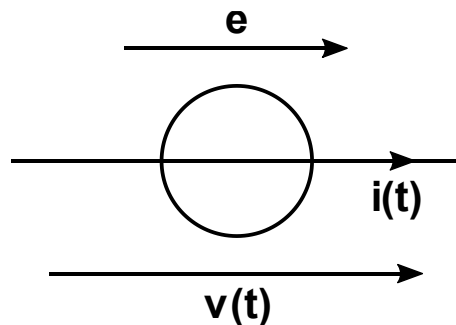
I - Reminders

Voltage generator

- A voltage generator is a dipole able to impose a constant voltage regardless of the current it supplies



$$v(t) = e, \forall i$$



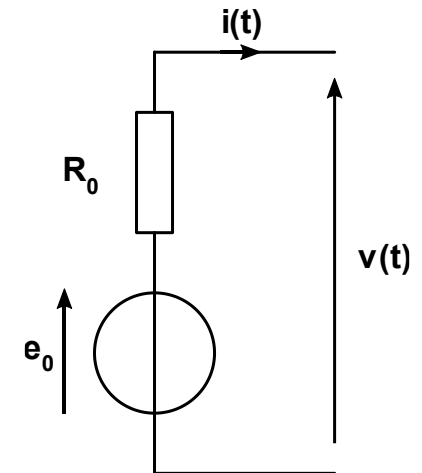
Thevenin model

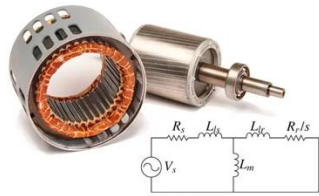
- Model used for the ideal voltage source
- Ideal voltage generator associated with a series resistor

No-load voltage: e_0
 Internal resistance: R_0
 Short-circuit current : $I_{CC} (v = 0)$

$$v(t) = e_0 - R_0 \cdot i(t)$$

$$I_{CC} = \frac{e_0}{R_0}$$

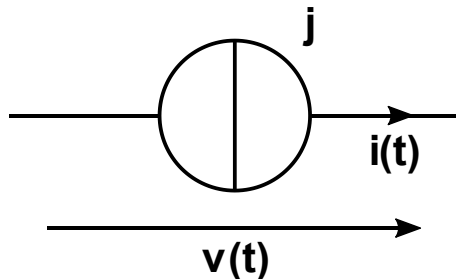
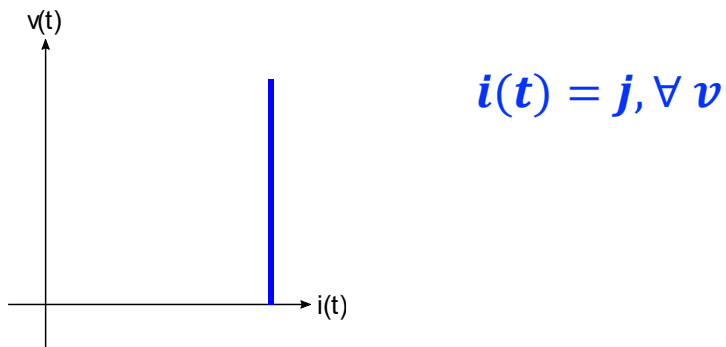




I - Reminders

Current generator

- A current generator that can impose a constant current whatever the voltage at its terminals



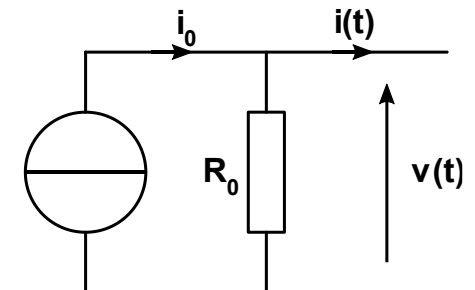
Norton model

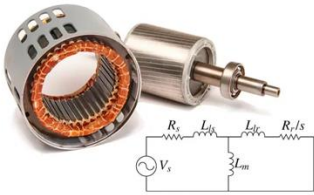
- Model used for the real current source
- Ideal current generator associated with a parallel resistor

Short circuit current: i_0
 Internal resistance: R_0
 No-load voltage: e_0 ($i = 0$)

$$i(t) = i_0 - \frac{v(t)}{R_0}$$

$$e_0 = R_0 \cdot i_0$$



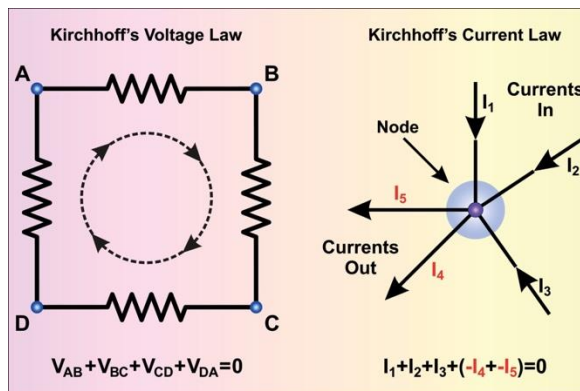


I - Reminders

Kirchhoff's laws

Definitions

- A **node** is a connection between more than two dipoles
- A **branch** is a portion of the circuit between two consecutive nodes.
- A **mesh** is a set of branches forming a closed path



Kirchhoff's current law

- The algebraic sum of currents arriving at a node is zero

$$\sum i_{entrant} = \sum i_{sortant}$$

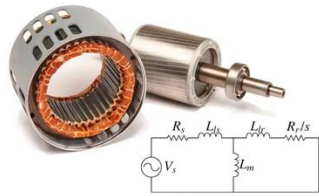
Kirchhoff's voltage law

- The sum of the voltages in a mesh is zero

$$\sum v_i = 0$$

Application rule

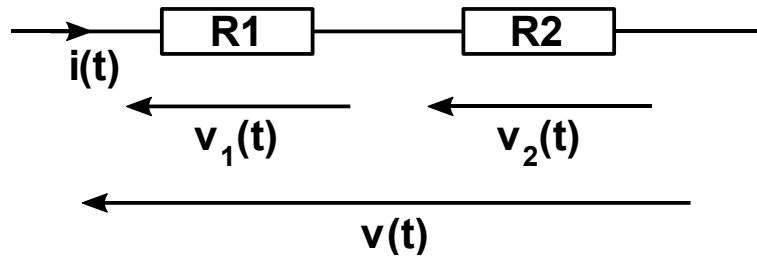
An arbitrary direction is chosen. The mesh is described in the chosen direction. Voltages in the same direction must be counted as positive, and voltages in the opposite direction must be counted as negative



I - Reminders

Divider bridges

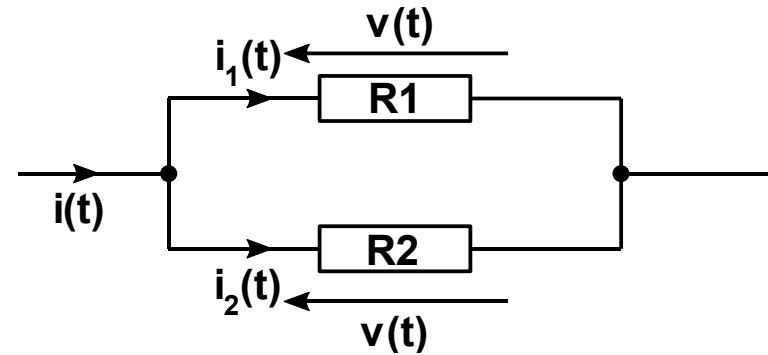
Voltage divider



$$v_1 = v \cdot \frac{R_1}{R_1 + R_2}$$

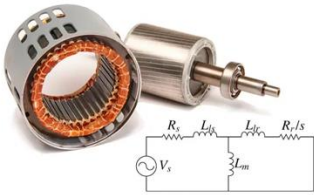
$$v_2 = v \cdot \frac{R_2}{R_1 + R_2}$$

Current divider



$$i_1 = i \cdot \frac{R_2}{R_1 + R_2}$$

$$i_2 = i \cdot \frac{R_1}{R_1 + R_2}$$



I - Reminders

Millman's theorem

For voltage generators

- n parallel voltage generators with resistance R_k and electromotive force e_k can be replaced by a single voltage generator with internal resistance R and electromotive force e

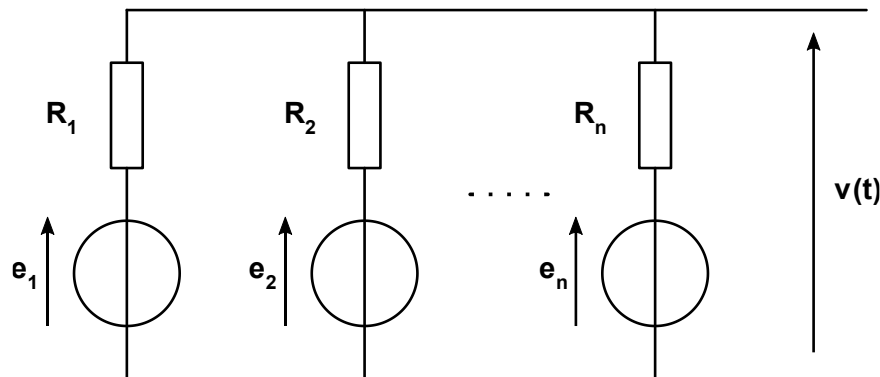
$$R = \frac{1}{\sum_{k=1}^n \frac{1}{R_k}}$$

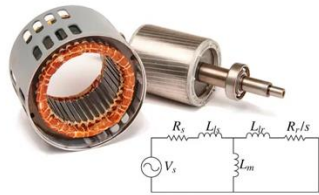
$$e = R \cdot \sum_{k=1}^n \frac{e_k}{R_k}$$

For a potential at one point

- Consider a current node of potential v in a network. This node is the junction point of n resistors R_k , subjected to potentials v_k on the other side of the node. The expression of the potential v is :

$$v = \frac{\sum_{k=1}^n \frac{e_k}{R_k}}{\sum_{k=1}^n \frac{1}{R_k}}$$

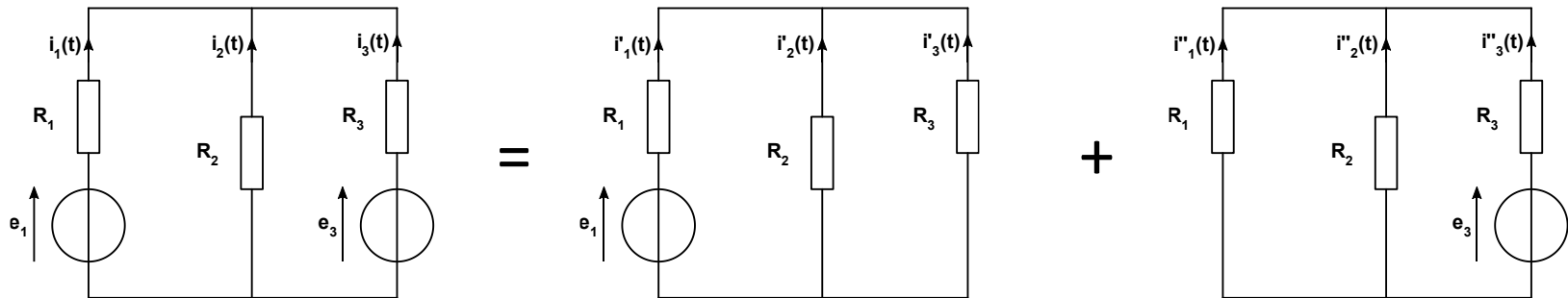




I - Reminders

Superposition theorem

- The **current** or **voltage** response of a network containing several independent sources acting simultaneously is equal to the **sum of the current or voltage responses** due to **each source** acting alone.



$$i_1 = i'_1 + i''_1$$

$$i_2 = i'_2 + i''_2$$

$$i_3 = i'_3 + i''_3$$